We present a fast, novel image-based technique, for reverse engineering woven fabrics at a yarn level. These models can be used in a wide range of interior design and visual special effects applications. In order to recover our pseudo-BTF, we estimate the 3D structure and a set of yarn parameters (e.g. yarn width, yarn crossovers) from spatial and frequency domain cues. Drawing inspiration from previous work [Zhao et al. 2012], we solve for the woven fabric pattern, and from this build data set. In contrast however, we use a combination of image space analysis, frequency domain analysis and in challenging cases match image statistics with those from previously captured known patterns. Our method determines, from a single digital image, captured with a DSLR camera under controlled uniform lighting, the woven cloth structure, depth and albedo, thus removing the need for separately measured depth data. The focus of this work is on the rapid acquisition of woven cloth structure and therefore we use standard approaches to render the results.

Our pipeline first estimates the weave pattern, yarn characteristics and noise statistics using a novel combination of low level image processing and Fourier Analysis. Next, we estimate a 3D structure for the fabric sample using a first order Markov chain and our estimated noise model as input, also deriving a depth map and an albedo. Our volumetric textile model includes information about the 3D path of the center of the yarns, their variable width and hence the volume occupied by the yarns, and colors.

We demonstrate the efficacy of our approach through comparison images of test scenes rendered using: (a) the original photograph, (b) the segmented image, (c) the estimated weave pattern and (d) the rendered result.
create these, and also allows for creation of detail at a range of scales for level of detail.

Our work is motivated by the material acquisition needs of the contract furniture business in which woven cloth model acquisition must be rapid, the volume of cloth swatches that need to be routinely processed is huge, and results must be renderable in high quality on a mobile device. Since our method is specifically designed to be used in this industry, where high quality renderings are necessary to show clients realistic representations of their newly designed interior spaces, this imposes high quality demands together with competing robustness and performance constraints and necessitating a fast approach. Our work is equally applicable to reverse engineering woven cloth models for other applications.

The desire to automatically recover a textile model for woven fabrics presents a number of challenges due to cloth appearance being dependent on both the structure and reflectance properties of the yarns used in the fabric. Self shadowing effects, weave pattern, variation in yarn widths, texture and loose fibres etc. contribute significantly to visual perception of variation and resulting visual richness of fabrics. Although woven cloth seems fairly regular in terms of structure, the yarns used can significantly impact upon the appearance of regularity. Consequently, to realistically recover a woven fabric model from an image we need to estimate the appearance of the yarns as well as the weave pattern itself.

![Fig. 2. Plain (a) and more complex weave patterns (b). Warps are the vertical yarns (colored gray), whereas wefts traverse horizontally (in magenta). The pattern is a binary matrix describing how warps and wefts are interlaced by a loom: 0 indicates the warp overlaps the weft at the corresponding yarn crossing, 1 means it lies below. The patterns are shown in the matrix.](image)

In recent years, within the computer graphics and vision research communities, there has been much interest in acquisition methods. A number of these works specifically focus on weave pattern recognition and synthesis of volumetric fabric appearance [Schwartz et al. 2013; Zhao et al. 2012]. Typically, these methods either rely on costly scanning equipment, are computationally intensive, or are data intensive [Schwartz et al. 2013]. Synthesized databases of various weave patterns are also expanding with the inclusion of new samples and typically require more storage space. Generation of new weave patterns from models within an existing database can reduce storage and typically require more storage space. Generation of new weave patterns from models within an existing database can reduce storage and hence expensive scanning equipment, are computationally intensive, or are data intensive [Schwartz et al. 2013].

Woven textiles possess spatially repeating structure defined by the warp and weft (Figure 2), which control the design and strength of the fabric. We hypothesise that, in common with crystallographic analysis [Thompson 1978], this regularity can be exploited to infer the weave pattern through Fourier domain analysis. Transforming an image into the frequency domain enables it to be expressed in terms of amplitude and phase of the frequencies contained within the original photograph and so the Fourier Transformed image signature will show clear peaks which can be used to understand the yarn crossover points in woven textiles.

Building upon this foundation, the four novel contributions of this paper are:

1. An algorithm to address inhomogenous fabrics (i.e. not all yarns with the same color);
2. An algorithm to address specific cases such as homogeneous and dark fabrics, for which the Signal to Noise Ratio (SNR) does not allow a proper analysis of the woven structure;
3. A noise model characterizing the noise from real sample textiles (i.e. variations in yarn width, misalignments, etc.);
4. An algorithm to insert the observed noise parameters from real samples into the generated depth maps;

Prior to discussing related work, we present an overview of our image processing pipeline to provide context for the discussion of the relative merits and limitations of previous approaches and to clarify the novel aspects of our work.

## 2 PIPELINE OVERVIEW

Our software takes as input a photograph of a fabric sample, captured with a standard DSLR camera. In common with other approaches we assume that the entire weave pattern repeat is contained in the photograph of the swatch. Although some exceptions exist, this condition is comparatively easy to obtain for a broad range of woven fabrics.

Recall that the visual characteristics of woven textiles are highly influenced by their resulting structural properties: fabric production machinery and the spinning technology of yarn production further complicates this causing an irregular distribution of warp and weft of yarns, which can result in skewed, twisted or partially overlapping yarns attributable to the slightly variable yarn width. For these reasons, we observe that naively analyzing the Fourier spectrum of images of woven cloth is insufficient for a robust algorithm.

This necessitates our novel multi-step approach (outlined in Figure 3) consisting of the following serial steps:

**Data Capture** Acquire input from textile swatches.

**Initial Image Processing** For each swatch, align axis yarns. Construct Fourier Signatures to use as unique identifiers.
and store these in a database. Automatically classify the input swatch into homogeneous or inhomogeneous.

**Inhomogenous Fabric Analysis** Apply our novel weave pattern detection and noise estimation algorithms described in Section 4.3. Save output to our own database for matching irregular (homogeneous) samples. Automatically classify the input swatch into homogeneous or inhomogeneous samples.

**Homogenous Fabric Analysis** Match to samples in database to deal with fabrics that are constructed from a single yarn color.

**Depth Map Creation** Create the 3D structure from the weave pattern incorporating the noise model to represent the natural yarn variations; derive a depth map from the 3D representation. Create an approximate albedo map.

In the following section we discuss related work. There is a large body of literature on acquisition, rendering and synthesis of cloth. However, since our focus is primarily on techniques to recover woven cloth models from images, we constrain our survey of related works to this area alone.

3 RELATED WORK

The methods discussed in this section can be classified in terms of Fourier Transform (FT) based, spatial domain based and database indexing approaches. As can be inferred from Figure 3 above, our method spans all three of these categories.
the statistical distribution of yarn irregularities necessary for realism in the rendered output. However, these works are important, as we use this idea in our work purely as an initial bootstrap step to construct a first guess about yarn crossings and their spacing.

A recent work by Schröder et al. is the closest current work to the algorithm we propose [Schröder et al. 2015]. The authors capture local irregularities such as thinning and thickening of yarns also using a single image as input. They also model the woven textile structure together with yarn parameters. Their method uses an iterative process starting with an estimate of the weave repeat obtained through autocorrelation analysis. Next they apply optical flow to register a tiled image of the weave pattern repeat to a shear corrected input image. This process is applied at both coarse and fine levels of granularity to locate yarn deformations. Horizontal and vertical structures are detected using cylindrical filters with an a priori requirement of size. The algorithm uses belief propagation and expectation maximization, on a graphical model, in which each node has a four-connected neighborhood. The textile image is then segmented using information from previous steps, assuming that yarns can be represented as tubes and minimizing a function which accounts for yarn color, background color and edge position.

Our approach, and the work by [Schröder et al. 2015], both aim to fully reverse engineer models of woven cloth at the yarn level. There are some elements in common purely because both algorithms address the same problem of recovering woven cloth models from a single image. However, Schröder et al. adopt a spatial domain approach. In contrast to all the prior works mentioned, our novel approach spans all three categories in our literature classification. This results in some important advances over previous methods. First, our method is fast compared with that of Schröder et al.’s which (according to the authors) takes 30–45 minutes to process each sample [Schröder et al. 2015], whereas our method takes seconds to a few minutes. Unlike other methods, the creation of our database indexed through the Fourier Signature allows us to rapidly obtain all the required information for rendering by simply matching the feature vector derived from the Fourier spectra, thus bypassing all the possible sources of errors and speeding up the reverse engineering process. Unique to our method, we are also able to construct woven pattern depth maps in a generative fashion and match observations in our image captures to these generated patterns. This allows us to build up a rich variety of datasets without measuring every possible woven fabric pattern we may encounter. A summary of the differences between our approach and Schröder et al.’s is reported in Table 1.

### 3.3 Database Indexing Approaches

Zheng et al. proposed a weave pattern database indexing method, based on a smallest weave repeat unit. The authors suggest a classification of patterns into three categories: plain, twill and satin. Their algorithm uses the Fast Fourier Transform (FFT) to describe the distribution of the weave pattern crossover points, followed by an entropy based method to index each pattern. In contrast to our approach, theirs requires that weave patterns are manually classified by experts [Zheng et al. 2009].

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**Table 1. Main differences between the proposed algorithm for reverse engineering the cloth and Schröder et al.’s method.**

Computed Tomography (CT) scans were used by Zhao et al. to produce high resolution synthesized material models. The authors used CT scanning to acquire a database of volumetric 3D models of complex woven textiles. Their algorithm used photographs of fabric to recover albedo alone and fit this to the CT scanned volumetric model. The method is very effective for synthesizing large regions of fabric free from tiling artifacts, but is limited to modelling the appearance of a single type of yarn and can only reproduce textiles that have been previously scanned [Zhao et al. 2011]. In subsequent work, Zhao et al. [Zhao et al. 2012] generate new samples from similar or simpler exemplars of a textile. Since their algorithm is able to predict appearance of specific weave patterns, this method is very useful for generating volumetric models of complex and spatially varying woven textiles. Realistic close up renderings are achieved from two types input, the description of the material weave pattern, and a few examples of simpler fabrics. Their method allows quick creation of new exemplars of fabrics due to a fast synthesis algorithm. Our acquisition method shares the same limitation to woven patterns (i.e. as opposed to knitted textiles) and removes the requirement on CT scan data [Zhao et al. 2012]. In [Zhao et al. 2016] Zhao et al. fitted CT data to a procedural model built upon [Schröder et al. 2015], further augmented with a measurement-based flyaway fiber model.

To summarize, our approach advances the state of the art of woven fabric appearance estimation by: removing dependencies on expensive scanning equipment, relaxing the need for a priori yarn dimensions, increasing the variety of woven fabric patterns that can be estimated through our ability to generate and match to synthetic weave patterns, and considerably speeds up processing compared with alternative approaches as required in our pipeline for high volume fabric analysis for use in industry.
4 A NOVEL FABRIC MODEL RECOVERY PIPELINE

In the following sections we describe in more detail the stages in our pipeline, as previously outlined in Section 2.

Conceptually a woven fabric image can be viewed as the juxtaposition of a number of weave patterns, created by interlacing yarns with a limited number of colors, hence it should contain a significant amount of self-similarities. However, the appearance of real fabric images is affected by incident lighting, choice of acquisition device, and other factors such as dust and lint over the fabric sample. Hence, the image of a fabric will contain all these factors, making the automatic analysis of woven fabric challenging.

Our pipeline relies on the properties of the 2D Discrete Fourier Transform (DFT) $\mathcal{F}$ of the input image $I$ of size $M \times N$, which represents the image content as a sum of an infinite number of complex exponentials (sinusoids) with different frequencies, thus resulting in a suitable way to identify regular structures:

$$\mathcal{F}(u, v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} I(x, y) e^{-j2\pi(ux/M + vy/N)}$$

where $x = 0, \ldots, M - 1, y = 0, \ldots, N - 1$ and $u = 0, \ldots, M - 1, v = 0, \ldots, N - 1$ are the frequency variables which span the frequency domain. The power spectrum of the transform is directly related to the Bayesian probability that a sinusoidal frequency is present in the data [Fougère 2012]. Roughly speaking, repeating structures in the input data give rise to high energy peaks in the power spectrum of the DFT: the brighter the peak, the more frequently a repeating pattern is observed in the input data. The value of the transform at the origin of the frequency domain $\mathcal{F}(0, 0)$, called DC coefficient, is equal to $MN$ times the average value of $I(x, y)$.

Given the fabric formation process on a weaving machine, we consider the image of a fabric sample to be a linear combination of three different signals:

$$\mathcal{F}(I) = \mathcal{F}(I_r + I_l + I_n) = \mathcal{F}(I_r) + \mathcal{F}(I_l) + \mathcal{F}(I_n)$$

where $I_r$, $I_l$ and $I_n$ respectively are the ideal image of the fabric as it would appear if produced by a perfect loom and captured by a perfect acquisition device, the image of the irregularities introduced by the real loom and the image of the noise due to the acquisition device, dust, lint and so on. The second equality holds thanks to the linearity of the DFT.

It has been observed in previous work [Schröder et al. 2015] that individual repetitions of the weave patterns may not have the same size, yarns may be partially occluded by neighboring yarns. However, when averaging over several warped repetitions, the yarn level structure becomes clearly visible and allows us to handle the non-rigid deformations of the cloth. In probabilistic terms, this implies that if a big enough fabric sample is observed, then containing several repetitions of the weave pattern, the probability of observing data belonging to $I_r$ is higher than the probability of observing loom deformations and noise due to fibers and other factors. Similarly we observe that noise due to dust, lint and so on is spatially invariant and does not display regular structures, whereas the noise due to the loom and yarn friction (i.e. deformations of the fabric lattice) tends to display spatial regularities. Moreover, fine-scale details and noise in the spatial domain correspond to high frequency terms, far away from the DC coefficient and the weave pattern frequencies. From these observations we safely assume that the lowest non-zero energy carried by a frequency term in $\mathcal{F}(I_r)$ is greater than the highest energy associated with any frequency term in $\mathcal{F}(I_l)$. If we denote $\mathcal{T}_r(I_m)$ as the set of frequencies of the DFT of an image $I_m$ with associated energy greater than zero, we have that $\mathcal{T}_r(I_r) \cap \mathcal{T}_r(I_l) = \emptyset$.

The steps in our algorithm, devoted to separate the terms in Equation 2 and recover the textile model, are presented in pipeline order as this is the same as the processing order. We begin with our data capture setup.

4.1 Data Capture

We capture woven textile swatches using a consumer Nikon DSLR camera, fitted with a Nikon macro lens 105mm f/2.8 AI – s. The sample swatch is placed horizontally inside a hemispherical acquisition rig, employed to obtain uniform incident illumination. Note that any uniform illuminant could be used instead, and our method is not dependent on the use of our specific capture setup. The camera is placed 50 cm above and orthogonal to the sample. A set of round fiducial markers (with known size) are positioned at the corners of swatches, in order to recover the scale of the yarns. Although our algorithm does not require this scale information to reverse engineer the yarn model, we use it to obtain renderings with the correct scale of the woven cloth pattern. This extra information allows us to use different capture setups with similar lighting, by allowing proper scaling of all the samples in the same way, even when the camera distance to the sample differs (e.g. in close-up shots and for swatches with very fine threads). Images are saved in the camera’s raw format and white balancing is performed, taking into account the known and controllable color temperature of the illuminant and the gain of the camera CCD [Reinhard et al. 2008]. To correct for vignetting and variations in incident lighting along the sample, we simply capture a flat white reference which is used as a correction map to compensate for lens falloff. While only one photograph is required for weave pattern estimation, if desired, our pipeline allows optional acquisition of more images of the same sample with exposure variation, in order to recover a higher fidelity albedo map.

4.2 Initial Image Processing

In this section we describe a set of preliminary image manipulations carried out in advance of estimating the woven textile pattern. These include, image alignment, creating an albedo map and extracting a Fourier Signature.

4.2.1 Image Alignment. Since the capture process involves placing a fabric swatch on a surface, placement errors or discrepancies in the yarn orientations within the swatch orientation itself will result in the warp and weft directions in the input image $I$ not being perfectly aligned with the $x$ and $y$ axis of the image formation plane. Thus, we perform a rotation of $\alpha$ degrees to achieve the necessary
alignment for later stages in our algorithm. We exploit the properties of the Radon Transform (RT) [Deans 1983], which allows us to reconstruct a 2D function $f$, by calculating the line integral on the possible space of straight lines $l$ in $\mathbb{R}^2$ ($\mathbb{R}$ refers to the set of real numbers):

$$RT_{x, \phi} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) \delta(x \cos \phi + y \cos \phi - s) \, dx \, dy$$  \hspace{1cm} (3)

Where the line of integration is specified in polar coordinates $(s, \phi)$ and $\delta$ is the Kronecker delta.

As explained in Section 4, on the whole fabric image we expect to more frequently observe the regular structure of the weave pattern rather than the deformations due to the weaving process. This gives rise to regular peaks in the $u, v$ domain, hence applying the Radon Transform to the image of the log magnitude of the Discrete FT $F(l_e + l_i)$ is more reliable than applying it directly on the input image $l$. We search for peaks of the function:

$$\Gamma_l = \int RT_{x, \phi} \, (\log F(l_e + l_i)) \, ds$$  \hspace{1cm} (4)

For search, we employ the following criteria [Jafari-Khouzani and Soltanian-Zadeh 2005]:

$$\alpha = \arg \max \frac{d \sigma_\phi}{d \phi}$$  \hspace{1cm} (5)

where $\sigma_\phi$ is the variance of the projection of the Radon Transform at $\phi$. To remove the term $F(l_b)$ from Equation 2, before computing the DFT we convolve $l$ with a Gaussian mask $G$, to suppress the noise due to the acquisition device characteristics and lint, thus suppressing unwanted high frequency terms in the Fourier domain. The radius of the filter preserves the frequencies associated with $l_r$ and $l_i$, since the structural information of the weave pattern is encoded in the low frequency terms. The FT of $G$ is still a Gaussian, hence we can express the idea of this filtering with the following, where $\otimes$ denotes a spatial convolution:

$$\mathcal{F}(l \otimes G) = \mathcal{F}(l) \cdot \mathcal{F}(G) \approx \mathcal{F}(l_r + l_i)$$  \hspace{1cm} (6)

The log intensity image of the magnitude of $\mathcal{F}(l_r + l_i)$ is then filtered to further enhance the peaks and the projections along several directions are analyzed using the Radon Transform allowing estimation of $\alpha$. The input image $l$ is then corrected for unwanted rotation and further processed within the pipeline.

4.2.2 Fourier Signature (FS) Extraction. We want to find a compact way to characterize the relevant properties of a fabric swatch, namely its regular structure and the deformations introduced by the loom and the properties of the yarns. In particular, we aim to capture the systematic deformations introduced by the loom, i.e. those most commonly observed within the input picture, which carry a relatively high energy in the Fourier Domain.

The set of frequencies useful to characterize the fabric appearance hence includes the entire $\mathcal{F}(l_r)$ (i.e. the ideal regular structure of the fabric) and a subset of the highest ranking frequencies (in terms of associated magnitude in the power spectra) in $\mathcal{F}(l_i)$ (i.e. the most frequent loom deformations).

To extract the FS, we automatically select multiple square $N_x N$ pixel image patches (spanning the weave pattern) from random parts of the image and average the power spectrum of their FT. This is indicative of the variation of the signal across the image and particularly useful to boost the signal to noise ratio for dark swatches, which do not reflect enough light to the camera sensor. At this stage in the process, we do not know the weave pattern. Therefore we bootstrap the process via an initial assumption that the weave pattern repeat has unknown width $W_{w}$ and height $W_{h}$ (in pixels) and both are smaller than $N$. The highest ranking frequencies in the mean power spectra, in terms of their power, are selected such that the sum of their energy $E_{h}$ is a fraction $K$ of the total energy $E_{T}$ of the spectra. Using our dataset as a benchmark, we found that a suitable value for $K$ is 0.3, which maximizes the $F_{score}$ [Jijsbergen 1979] for samples retrieval. The $F_{score}$ is defined as:

$$F_{score} = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$  \hspace{1cm} (7)

The terms precision and recall can be defined as follows [Sokolova and Lapalme 2009]:

- **precision**: the number of correctly classified samples of a given class, divided by the number of examples labeled by the system as belonging to that class.
- **recall**: the number of correctly classified samples of a given class, divided by the number of samples of that class in the dataset.

![Fig. 4. Four textile samples (top row) and their respective FSs (bottom row). The samples depicted in (a) and (b) have the same weave pattern, notice the similarities between their FSs (respectively in (e) and (f)). The samples reported in (c) and (d) have the same weave pattern and similar FSs (see (g) and (h)).](image)

Natural irregularities in fabrics have implications on the shape of the FS, as can be seen in Figure 4. Each show two samples of the same cloth with their corresponding FS. Figure 5, shows the impact on the shape and intensity of peaks of the FS of a textile sample with black yarns.

We identify a suitable subspace to project the shape signature, by reducing the search space for features and so obtain a smaller set of feature vectors to be used for later classification. This is achieved by...
analyzing the Fourier Signatures using Kernel Principal Component Analysis (KPCA) [Schölkopf et al. 1998]. This extension of classical PCA is ideal for dealing with non-linear cases through a non-linear function $\Phi$, which maps the input space into a high dimensional feature space and then applies a linear method in the augmented function $\Phi$. PCA is ideal for dealing with non-linear cases through a non-linear function $\Phi$.

$\Phi$ is simply defined as:

$$\Phi(f_j) = \frac{1}{k} \sum_{i=1}^{k} \Phi(f_1) + \sum_{i=1}^{N_k} \phi_{j,i}^{\Phi} \phi_i$$

(9)

By varying the values of the set of $\phi_{j,i}^{\Phi}$ we can generate unseen shapes, a key aspect for enlarging our database to be used for homogeneous sample analysis. We select a subset of $q$ principal eigenvalues $\lambda_1^\Phi, \lambda_2^\Phi, \ldots, \lambda_q^\Phi$, such that they are able to explain the main variations observed in $\Phi$, with $d < N_k$ and:

$$\lambda_1^\Phi \geq \lambda_2^\Phi \geq \ldots \geq \lambda_q^\Phi \geq \ldots \geq \lambda_{N_k}^\Phi.$$  

(10)

The vector $v_j = [\phi^{\Phi}_{j,1}, \phi^{\Phi}_{j,2}, \ldots, \phi^{\Phi}_{j,q}]$ constitutes the FS of the fabric. In our experiments we selected a Gaussian kernel, with variance equal to 3 times the average distance between the samples in the feature space. The set $\mathcal{F}$ is constructed by analyzing a number of inhomogeneous fabrics through the pipeline described in Section 4.3, which also gives us the yarn parameters and weave patterns. Once $\mathcal{F}$ has been analyzed by KPCA and the FSs obtained, we can populate our database and associate each signature to the corresponding yarns and noise parameters derived through the pipeline. The number of elements in our database can be extended generatively, to create arbitrary samples that can be used to build up further exemplars in our database for enhanced matching.

Given two samples $f_i, f_j \in \mathcal{F}$, with FS being respectively equal to $v_i$ and $v_j$, their distance $D_{FS}$ is simply defined as:

$$D_{FS}(f_i, f_j) = \frac{|v_i \cdot v_j|}{\|v_i\| \|v_j\|}$$

(11)

A database query triggers the calculation of the distances between the input sample and all the others stored in the database; the sample with the smallest distance is then retrieved from the database and its parameters can be used for the depth map and albedo estimation.

To determine if a sample is homogeneous, our algorithm automatically analyzes the histogram of $I_r$ in order to locate the number of peaks; each peak is the initial estimate of a color cluster center. The distance between each pair of neighbouring clusters is computed, and if it is less than an empirically determined threshold (determined using a data set of 20 samples) the two clusters are merged and a new cluster center is computed. This process is repeated until no more clusters can be merged; if only one cluster is left the sample is labelled as homogeneous.

### 4.3 Inhomogeneous Fabric Analysis

In this section we detail the algorithm for inhomogeneous fabrics, which takes the primary processing route as shown in Figure 3. These fabrics are fairly regular and have two or more colors of yarns. We begin by describing how we determine the warp, weft, crossover points and yarn dimensions. The proposed pipeline for this stage of the algorithm is described in detail in the following section.

#### 4.3.1 Weave Pattern Detection.

We aim to segment the fabric image using a set of features which includes the color, hence the aforementioned factors need to be handled using low-level image processing techniques both in the frequency and spatial domains. From the segmented image, it is possible to exploit self-similarity to identify repeat patterns in the fabric sample.

Recall that the regular structure of a fabric sample, contained in the image $I_r$, should be clearly noticeable in the frequency domain, where the brightest peaks give information about the fundamental frequencies related to the thread density in weft and warp directions.
Higher frequency terms without associated high energy can be explained by noise and fine details, contained in the image $I_{w}$, filtered in earlier stages of our pipeline (see Section 4.2.1) by means of a convolution with a Gaussian kernel $G$.

From Equation 6, taking into account the assumptions described in Section 4 we can obtain $F(I_{r})$ from $F(I_{r} + I_{l})$. An automatic selection of the peaks (i.e. strong local maxima) in $F(I_{r} + I_{l})$ is performed and each of them is added to the set of frequencies of $F(I_{r})$; thanks to the symmetry property of the DFT, the search space in the frequency domain is reduced to $1/2$, since the symmetric point of a peak in the frequency domain is also a peak (more precisely the real part is symmetric and the imaginary part is anti-symmetric). We do not search for a predefined number of peaks, as this would put a limitation on the typology of fabric we can handle. Instead, we aim to add as many strong peaks as possible, by thresholding the gradient values of the magnitude of the DFT to the 99.8 percentile of the gradient values. From the set of peaks we select the one(s) with the minimum energy, which gives a threshold to discriminate the frequencies in $F(I_{r})$ from the frequencies in $F(I_{l})$.

We can finally derive the estimate of the ideal fabric image $I_{r}$ simply as $F^{-1}(I_{r}) \circ G^{-1}$, where $G^{-1}$ is the high-pass kernel obtained as the inverse of $G$. The described procedure is repeated for each color channel individually, combining the per channel estimated into a single RGB image. Examples of $I_{r}$ are shown in Figure 6.

![Image](a) Input image (b) Ideal image $I_{r}$ (c) Input image (d) Ideal image $I_{r}$

Fig. 6. Two fabric swatches (6(a) and 6(c)) and their corresponding estimated ideal images $I_{r}$ (6(b) and 6(d)).

Under diffuse lighting we obtain a photograph of the fabric swatch from the normal direction, in which the centers of the yarns have the highest intensities and the intersections between yarns appear dark [Schröder et al. 2015]. This is particularly clear by analyzing $I_{r}$ (see Figure 6), where the noise and the sharp specular highlights have been filtered out and enables us to derive a first estimate of the position of these intersections by examining the local minima of the projection profiles, along both the horizontal and vertical directions, of the ideal model of the fabric image. The projection profiles are calculated from the gradient values, since they allow us to obtain a more reliable estimate of the regular grid of yarn intersections.

At this stage in the algorithm, we now have a set of estimated intersection positions such that a yarn passes through two neighboring ones (i.e. their distance defines the yarn width). We model the relative set of yarn widths as gamma distributions (one per yarn color) filtering out the outliers. We roughly partition the image into a set of strips, each of which contains one weft. By measuring the distance between each pair of strips, we obtain a matrix of distances. The basis for this is that the minimum distance between the image of a weft (with all the warps going over it) and another one is achieved periodically, when the weave pattern repeats itself. We employ the Image Euclidean Distance (IMED) [Wang et al. 2005], a variation of the classic Euclidean distance which proves to be robust to local deformations by taking into account the relative position of pixels by considering the angles between them.

Let two images $x$ and $y$, of size $M \times N$, be $x = (x^1, x^2, \ldots, x^{MN})$ and $y = (y^1, y^2, \ldots, y^{MN})$, where $x^k$ indicates the gray value in image $x$ at location $(k, l)$. Their IMED distance $d(x, y)$ is given by

$$d^2(x, y) = \frac{1}{2\sigma^2} \sum_{i,j=1}^{MN} \exp\left(-\frac{|P_i - P_j|^2}{2\sigma^2}\right)(x^i - y^i)(x^j - y^j),$$

where $|P_i - P_j|$ is the distance between pixels $P_i$ and $P_j$ on the image lattice. Through examining the resulting matrix, we are able to locate the diagonals which show the lowest cumulative values. The distance between them gives us the number of wefts $N_{w}$ in the weave pattern; an example is shown in Figure 7. This process is repeated for warps, obtaining their number $N_{a}$. From this we extract the weave repeat which enables us to roughly partition the image in terms of the elementary weave repeat pattern of size $N_{w} \times N_{a}$.

![Image](a) Distance Matrix (b) Normalized cumulative distance along diagonals

Fig. 7. Distance matrix among wefts in a sample area of Figure 4(a) and (b), left side. Due to symmetry, only the upper triangular part needs to be calculated. The plot of the normalized cumulative distance on the right, calculated along the diagonals, refers to the upper triangular matrix (i.e. diagonal 0 is the main diagonal).

As previously mentioned due to yarn and loom characteristics, the distribution of the yarns is irregular in the input image $I$. The estimated yarn arrangement thus requires further refinement to match the observed input image of the fabric. We aim to deform the regular grid obtained from previous steps by analyzing $I_{r}$ to achieve a good match with the crossed areas of warp and weft yarns. The center positions of each cell in the regular grid are used to seed region growing [Adams and Bischof 1994] and the features we use for the algorithm are the CIELAB [Wyszecki and Stiles 1982] color values from the original input image. For the distance metric, we use the $\Delta E_{90}^{*}$ color difference formula, with a merging threshold set to $\Delta E_{90}^{*} = 2.3$ defined as the Just Noticeable Difference (JND) [Sharma 2002].

Each of the regions found in the previous step form an irregular grid $N_{w} \times N_{a}$, in which each cell encloses a weft/warp crossing. To determine whether it is the warp passing over the weft or vice versa, we analyze the texture features in a rectangular fixed window around
We will inevitably encounter sample textiles for which the above technique cannot be used to determine weave patterns, due to the large variation of types of yarns and colors used in woven fabrics. In particular, we found homogenous fabrics to be challenging as well as those with dark colored yarns. To handle these cases, we take the second route through our pipeline overview (shown in Figure 3) instead.

We derive the FS of the sample and search our database for the closest match of woven pattern among the data saved from previously encountered samples and assign the associated depth map parameters to the recovered model for the input sample. The distance measure is given by the angular similarity between the input FS and the candidate’s FS in the dataset. An ideal match would find the same weave pattern and allow to use the previously stored parameters to synthesise the depth map; if the same weave pattern has not been stored previously, the parameters associated with the FS displaying the highest angular similarity in the dataset will be retrieved. For a densely populated dataset, this would mean to retrieve the most similar weave pattern.

Recall that we build a database including the estimated weave patterns and the inferred depth maps from all our samples. This contains the FS of weave patterns for every sample we encounter, extracted by examining the highest ranking frequencies in the Fourier Transform of the input fabric image. For matching purposes, and dimensionality reduction, we perform Kernel Principal Component Analysis (KPCA) on the space of signatures to obtain a small feature vector storing just the first N main modes. This allows for optimized lookup as the entire signature for each pattern is not stored.

In addition, we can also procedurally generate synthetic depth maps for woven fabrics using any arbitrary weave pattern, plausible yarn parameters, and noise with typical observed values for a class of materials. This enables us to obtain a FS matching those extracted from photographs of a real fabric woven with a similar yarn and employing a similar weave pattern to the one simulated. Once our database has been sufficiently populated (with at least 30 samples), we can simply use the photograph of the challenging swatch to extract its FS and query the database using its first NK KPCA modes as a feature vector. In order to derive a dataset with a reasonable size we analysed the fabric samples provided by KisP Inc. and found out that the most common weave samples have very similar weave patterns, hence we used them to bootstrap our database. Consequently, we are able to robustly assign a depth map to samples that cannot be reliably analyzed.

### 4.5 Depth Map Creation

![Depth map generation](Image)

**Fig. 8.** Depth map generation.

![Depth map examples](Image)

**Fig. 9.** Depth map examples; from (a) to (c) the maps are obtained by re-injecting larger subsets of the estimated noise parameters.

From the parameters estimated in the previous step (weave pattern, yarn width, gaps among warp and weft) we can extract a regular
Page 10: A fabric swatch with a 8 × 24 weave pattern; Row 2: A fabric swatch with a 6 × 10 weave pattern; Row 3: A fabric swatch with a 6 × 6 weave pattern. The estimated minimal weave patterns in 10(d), 10(k), 10(r), refer to the areas highlighted in blue respectively in 10(b), 10(i), 10(p), scaled to a 1:1 ratio between width and height.

4.5.1 Normal map and Albedo Map. For many materials the visual complexity is mainly due to the geometric complexity, rather than the actual reflectance [Magda and Kriegman 2006] and the use of relatively simple albedo map estimation procedures has been demonstrated and perceptually validated for textured surfaces [Glencross et al. 2008] and planar samples [Riviere et al. 2016].

To estimate the diffuse albedo we first derive the surface normals at the yarn level, which have been previously approximated with the micro-cylinders (see Section 4.5). The knowledge of the surface normals allows us to account for the cosine foreshortening. We assume that a thread cannot change color along its path and it is made of homogeneous fibers with the same color. Hence, for each thread, the median of the estimated intensities provides us with the diffuse albedo, whereas the top 20% of the intensities is used for the specular level. Finally, we add 3D Perlin Noise [Perlin 1985] to the micro-cylinder derived normal map, to visually simulate the effect of the yarn fibers. If a higher quality albedo map is desired, we capture seven exposures of the swatch over a range of 3 f-stops and combine these using Greg Ward’s command line high dynamic range image builder [Ward 2001].

4.6 Renderings

If the input fabric shows a reasonable amount of specularities this does not pose a problem to our pipeline. If the cloth is very shiny and specular, then cross-polarized photography could be used to capture the input sample.
At this stage we have an albedo map, a specular level, normal map and a depth map for our fabric sample, which we render using Autodesk 3ds Max, although any rendering algorithm could be used. The light model we used is a Target Directional Light, which casts parallel light rays in a single direction, as this approximates well the light sources installed in our acquisition setup. We used an anisotropic BRDF model and set the Index of Refraction to 1.4 if information about the fibers used for the threads was not available.

5 RESULTS AND EVALUATION

We demonstrate the effectiveness of our pipeline using four textile samples processed through the inhomogeneous fabric pipeline, acquired from fabric swatches exhibiting very different weave patterns, yarn colors, and weave repeats. Specifically, $8 \times 24$ (welts $\times$ warps), $6 \times 10$, $6 \times 6$ and $24 \times 100$ weave pattern swatches have been used. In the first three cases, we show that the weave pattern has been correctly recognized as can be seen in Figure 10. One row of the weave pattern, in the fourth sample (shown in Figure 11) has been misclassified. However, the generated depth map and corresponding rendering are not negatively affected due to the small size of the missing row compared with the weave pattern.

To evaluate the visual accuracy of our recovered textile model, in Figure 12, we show comparisons between our rendered images and photographs of the same fabric samples under identical lighting conditions. From the estimated depth map of the fabric we create Normal/Displacement/Bump Maps to use for the renderings. Our estimated noise, yarns and weave patterns have been used for all the renderings. In Figure 15 we show the renderings of recovered textile models, mapped on the surface of a cylinder to show the benefits of the depth map; close up images are shown in the insets. Recall that the effectiveness of the Fourier Signature was previously demonstrated in Figure 4 which shows that the same weave pattern can be easily recognized and that the Fourier Signature is very different for different classes of swatches. Moreover a completely black swatch, which cannot be correctly classified with our inhomogeneous fabric pipeline is correctly classified using our homogenous pipeline and shown in Figure 5; in Figure 13(e) we report the rendering for this swatch, in which the albedo estimation is negatively affected by the very dark color and low signal-to-noise ratio. We also included the results obtained by analyzing two more fabric swatches, other than the aforementioned black one, through the homogenous fabric pipeline (i.e. using the FS to retrieve the best matching parameters from our database). The ground truth photographs and the rendering are reported in Figure 13. In particular, Sample 5 (Figure 13(a)) contains only one full repetition of its $48 \times 200$ weave pattern and our pipeline is not able to robustly estimate it; the use of the database allows use to find a close matching in Sample 4 (Figure 11(a)) and from this derive the model parameters. As for Sample 6 (Figure 13(c)), its weave pattern is ambiguous and even with a careful visual inspection it is not possible to determine the number of repetitions: however, our homogeneous fabric pipeline found the closest matching sample in the database and estimated a suitable model in about 29 seconds. In Table 2 the processing times for each of the samples is reported, estimated using an unoptimized single-core Matlab implementation on a laptop. Finally, we also compare with a recently published alternative method proposed by Schröder et al. [Schröder et al. 2015], using the same fabric photographs (kindly provided by the authors).

In Figures 12, we show the resulting correctly estimated weave patterns and corresponding renderings, it is important to note that these are for visual comparison only. These images are rendered under uniform lighting and by visually matching parameters (such as the camera lens and distance to the swatches) as the complete set of rendering and modeling parameters are not reported in Schröder et al. [Schröder et al. 2015]. $I_r$ is the simplified image (ideal loom, perfect acquisition).

<table>
<thead>
<tr>
<th>Sample ID</th>
<th>Number of weave repeats</th>
<th>Processing time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sample 1 (Figure 12(e))</td>
<td>90</td>
<td>375 sec</td>
</tr>
<tr>
<td>Sample 2 (Figure 12(i))</td>
<td>443</td>
<td>85 sec</td>
</tr>
<tr>
<td>Sample 3 (Figure 12(a))</td>
<td>201</td>
<td>132 sec</td>
</tr>
<tr>
<td>Sample 4 (Figure 11(a))</td>
<td>9</td>
<td>318 sec</td>
</tr>
<tr>
<td>Sample 5 (Figure 13(a))</td>
<td>1</td>
<td>55 sec</td>
</tr>
<tr>
<td>Sample 6 (Figure 13(c))</td>
<td>Unknown</td>
<td>29 sec</td>
</tr>
<tr>
<td>Sample 7 (Figure 13(e))</td>
<td>190</td>
<td>47 sec</td>
</tr>
</tbody>
</table>

Table 2. Processing times for estimating a fabric model for the sample reported in Figures 11-13, excluding renderings. Samples 1-4 have been processed through the inhomogeneous pipeline, whereas samples 5-7 through the homogenous pipeline.

6 LIMITATIONS

Our algorithm assumes that our capture is performed under diffuse lighting, the entire weave repeat is contained within the image, the camera position is fixed, and the sample swatch is planar without significant deformations. Consequently, our approach has some limitations. First the input image needs to contain the whole weave pattern repeat in order for our algorithm to obtain a robust Fourier Signature that is invariant to translations and rotations of the samples. The second limitation is that for our voting algorithm to properly classify the patterns observed in the swatch, we require multiple observations in the image, similar to [Schröder et al. 2015], meaning that the weave repeat needs to be small with respect to the size of the captured swatch. Third, in common with other methods [Schröder et al. 2015; Zhao et al. 2012], we currently cannot estimate woven fabric.
patterns for textiles that do not observe a grid like woven structure, such as knitted textiles. The first two limitations can be addressed in future work by incorporating automatic techniques to stitch together photographs of sub-areas of the sample textile [Brown and Lowe 2007; Szeliski 2010] or by generating synthetic woven patterns that are larger than a swatch and matching an observed portion to the larger pattern structure. The third limitation can be addressed in future work by using a von Mises distribution instead of the current integral projection used in our implementation [Dhillon and Sra 2003].

Finally, unlike Schröder et al [Schröder et al. 2015], although we capture a volumetric model of the woven cloth (inferring the yarn path and volume) we do not model the light scattering at the fibre level. Our target application, necessitates certain trade-offs when compared with the work of Schröder et al. [Schröder et al. 2015]. While modeling the light scattering at the fibre level leads to a boost in visual quality, it is not critical for our application in Virtual Reality visualization of interiors for the contract furniture industry. However, conceptually, there is nothing preventing our algorithm from being extended in this way.

7 CONCLUSIONS

To conclude, we have demonstrated a pipeline for reverse engineering 3D textile models of woven fabrics, we have presented four novel algorithms within our pipeline to extract volumetric fabric models using a single image as input. Our method computes a model in up to a few minutes. The creation of our database indexed through the Fourier Signature allows us to rapidly obtain all the required information for rendering by simply matching the feature vector derived from the Fourier spectra. We are also able to construct woven pattern depth maps in a generative fashion and match observations in our image captures to these generated patterns. This means that our algorithm can build up a rich variety of datasets without needing to measure every possible woven fabric pattern we may encounter. Consequently, we can also generate woven patterns that are larger than a swatch and match an observed portion to the larger pattern structure. This means that our method is more suited to its target application in the contract furniture industry, in which thousands of swatches needs to be rapidly classified and might share the same weave pattern but have different colors. In particular, this also allows us to deal with completely black samples, provided a similar weave pattern has been previously classified. The results of our estimation pipeline are illustrated using several woven textile samples, containing very different weave patterns and yarns. We also compare with ground truth data and also with previous similar work. We have highlighted
Weave repeat.

limitations of our methods and also propose solutions to these. If sufficient numbers of fabric swatches are characterized (captured and/or synthesized), then our solution for homogenous textiles could be used exclusively for fast inference of the textile model from a photograph of any woven fabric swatches.

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Fig. 15. Woven fabric models shown on a cylinder for illustration. (a) Rendering of the fabric shown in Figure 10(a); (b) Rendering of the fabric shown in Figure 10(h); (c) Rendering of the fabric shown in Figure 10(o);